

# Estimating Equity Premia from CDS Spreads

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## Abstract

We propose a new approach to estimate the equity premium using CDS spreads and structural models of default. Our estimates yield equity premia of 6.50% for the U.S., 5.44% for Europe and 6.21% for Asia based on 5-year CDS spreads from 2003-2007. Due to some conservative assumptions these estimates are upper limits for the equity premium. Using 3-, 7- and 10-year CDS maturities yields similar results and offers an opportunity to estimate the term structure of risk premia. Although our estimator is developed in a Merton framework it is robust with respect to model changes. In fact, we obtain similar results when extending the approach to a first-passage-time framework, strategic default frameworks or a framework with unobservable asset values (Duffie/Lando (2001)).

**Keywords:** equity premium, credit risk premium, credit risk, structural models of default  
**JEL classification codes:** G13, G31

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## I Introduction

Risk premia in equity markets are a widely researched topic. The risk premium in equity markets is usually defined as the equity premium, e.g. the excess return of equities over risk free bonds. The literature discusses three different ways for the measurement of the equity premium: Models based on historical realizations, discounted cash-flow models and models based on utility functions. While historical averages have long dominated theory and practical applications, current research suggests an upward bias for the U.S. market, e.g. the ex post realized equity returns do not correctly mirror the ex ante expected equity premium. Among other things, this can be explained by survivorship bias, risk premium volatility, enhanced diversification possibilities, changes in interest rate levels and states of the economy; cf. for example Illmanen (2003) and Fama/French (2002). In the U.S., historical averages have been around 7 to 9% depending on the time horizon and methodology (arithmetic/geometric averages) used (cf. Fama/French (2002) and Ibbotson (2006)). Discounted cash-flow models have become more popular recently, but are also subject to debate, in particular for their high sensitivity to forecasts of dividend- or earnings growth rates. Estimations based on such models yield implied equity premia in the range from 1%-9%, cf. Claus/Thomas (2001), Gebhardt/Lee/Swaminathan (2001), Fama/French (2002), Gode/Mohanram (2003), Easton et.al. (2002) and Easton (2004). Approaches based on utility functions have been subject to intensive debate in the academic literature - mainly based on the 'Equity Premium Puzzle' put forward by Mehra/Prescott (1985). Within this approach risk premia larger than 1% can hardly be derived, however, its importance for practical applications can currently be neglected.

It is obvious that risk aversion of investors influences both credit prices and returns as well. As an example, we have collected information about credit default swap (CDS) contracts of A-rated obligors in the CDS-index CDX.NA.IG from 2003-2007. The average 5-year CDS spread has been 37 bp, whereas the average annual expected loss (EL) is only appr. 9 bp. Therefore, these 5-year CDS investments yield an average return of appr. 28 bp (= 37 bp - 9 bp) above the risk free rate, as can be seen from Table I. In absolute terms, this premium increases with decreasing credit quality, i.e. the expected net returns increases with increasing riskyness. Measured relative to the expected loss (or the actual default probability) it decreases with declining credit quality. Over the last years, research on this default risk premium has developed, but there has not yet emerged consensus on the methodology for measuring these default premia. Current approaches mainly use simple ratios or differences between risk neutral and actual default probabilities, cf. for example Berndt et.al. (2005) and Hull et.al. (2005).

We use structural models of default to convert credit spreads into an equity premium. Specifying a specific structural model, one can derive the risk neutral and the actual default probability. Used the other way around, the difference between risk neutral and actual default probability yields

Rating grade	Average 5-y-CDS-mid (bp)	Average 5-y-EL p.a. (bp)	$\Delta$ (bp)	Q-to-P
AA	31.53	5.23	26.30	6.03
A	37.37	9.17	28.20	4.07
Baa1	48.43	14.60	33.83	3.32
Baa2	56.91	22.00	34.91	2.59
Baa3	68.51	33.17	35.34	2.07

Table I:

**Credit risk premia**

Credit risk premia for 5-year CDS (Index CDX.NA.IG, 2003-2007) based on Moody's rating and a recovery rate of 45%.  $\Delta(bp)$  is the difference in bp between 5-year-CDS spread and 5-year-EL p.a. (based on historical data per rating grade). Q-to-P is the ratio of CDS spread to EL p.a.

the dynamics of the asset value process, in particular the asset Sharpe ratio. Together with the asset correlation and the implied volatility, we are then able to derive the market Sharpe ratio and the equity premium. Our approach is probably most similar to Bohn (2000), Agrawal/Arora/Bohn (2004) and Huang/Huang (2005). Our contribution is threefold: First, we use a closed form solution for the estimation of the market Sharpe ratio and the equity premium derived in a Merton framework. Moreover, we extend this estimator to first-passage-time-models, strategic default models and models with incomplete information based on Duffie/Lando (2001). To our best knowledge this has not been done in the literature yet. Second, we apply the estimator to more than 150,000 CDS spreads from the major CDS indices in the U.S., Europe and Asia. Using CDS helps to mitigate the 'risk-free-rate-problem' (c.f. Hull et.al. (2004)), i.e. we do not have to estimate the correct corresponding risk-free rate. By using constituents of a liquid CDS index we avoid the 'size-problem'<sup>1</sup> and should be less exposed to liquidity risk issues. Third, we perform a rich set of robustness tests including different specifications for the real world default probability based on hazard rate models.

The estimator of the market Sharpe ratio and the equity premium derived in this paper has three important characteristics which make it very convenient. First, it is only based on observable parameters, i.e. risk neutral and actual default probabilities, the maturity and the equity correlation. The risk neutral default probability and the maturity can be derived from CDS spreads, the actual default probability from ratings<sup>2</sup> and the correlation from equity prices. Unlike other applications of structural models, we do neither have to calibrate the asset value process nor the default barrier. Second, the estimator is robust with respect to model changes. We examine a classical first-passage-time-model and the Duffie/Lando (2001) model which incorporates strategic default and unobservable asset values. Third, the estimator is robust with respect to

<sup>1</sup>Various literature has pointed out to the fact that size plays a role in (expected) returns and Sharpe ratios, c.f. e.g. Fama/French (1993, 1996). There are also indications that the size effect plays an important role in credit markets as well, c.f. Agrawal/Arora/Bohn (2004).

<sup>2</sup>We use EDFs (expected default frequencies) from Moody's KMV and - as a robustness test - agencies (Moody's/S&P/Fitch) ratings and a multi-period hazard rate model.

noise in the input parameters. As an illustration, we look at a model-based 5-year spread of a BBB-rated obligor. This credit spread is 37 bp for a company Sharpe ratio of 10%, it is 140 bp for a company Sharpe ratio of 40% (cf. subsection II.A for a detailed analysis). This large difference indicates that common noise in the data<sup>3</sup> will not significantly reduce the possibility to extract the Sharpe ratio and the equity premium out of credit spreads. Mathematically, the sensitivity of the model-based credit spread with respect to the Sharpe ratio is 'high' compared to other noise in the data.

We have applied our equity premium estimator to the constituents of the main CDS indices in the U.S. (from 2003-2007) and for Europe and Asia (from 2004 to 2007). The risk neutral default probability was derived from CDS spreads, EDFs (expected default frequencies) from KMV were used as the primary source for the actual default probability.<sup>4</sup> We estimate equity premia of 6.50% for the U.S., 5.44% for Europe and 6.21% for Asia. Due to some conservative assumptions<sup>5</sup> these estimates are upper limits for the equity premium. This confirms former research that the historical equity premium is upward biased. The results are quite stable over time, e.g. for the U.S. equity premia estimates range from 5.16% in 2004 to 7.18% in 2005. Using different CDS maturities (3-, 7- and 10-year) to estimate the equity premium also results in similar - though slightly smaller - estimates for the equity premium. Our approach could also be used as a starting point to estimate the term structure of risk premia.

The remainder of the paper is structured as follows. Section II describes the theoretical framework for credit risk premia based on asset value models. We examine a classical Merton model, a first passage time model and a model based on unobservable asset values as proposed by Duffie/Lando (2001). Section III describes our data and provides descriptive statistics. The equity premium estimates for the U.S based on 5-year CDS are reported in section IV, results from other maturities (3-, 7- and 10-year) and other markets (Europe and Asia) are reported in section V. To confirm the robustness of our results, we conducted extensive sensitivity analysis which we report in section VI. Section VII concludes.

## II Model setup

The basic idea is to measure the excess return on debt and postulate a model linking debt valuation to asset valuation and asset valuation to equity valuation. Excess returns on debt instruments can then be transformed into excess returns on equity instruments. Technically, we use structural

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<sup>3</sup>E.g. bid-ask spreads, liquidity effects and inaccuracies in determining the actual default probability.

<sup>4</sup>Please note that EDFs from KMV are not calibrated based on KMV's assumption about the asset drift / equity premium but based on historical data. Therefore there is no circular statement in our arguments. In addition, various robustness tests are performed.

<sup>5</sup>In particular we assume that 100% of the CDS spread is attributable to credit risk.

models of default to derive a relationship between risk neutral and actual default probabilities. Empirically, most structural models perform poorly, cf. Eom et.al. (2000). One of the main reasons is the calibration process usually needed to specify structural models, e.g. determination of leverage, asset volatilities etc. In contrast to mainstream literature, we do however not aim to derive actual and risk neutral default probabilities from structural models. We are simply interested in the relation between risk neutral and actual default probabilities. Hence, we simply assume that there exists a structural model that yields the correct actual default probability and from there we derive the risk neutral default probability. It is therefore not necessary to perform the calibration process that is usually required. Our approach is probably most similar to Huang/Huang (2005) and Bohn (2000). Our approach differs though in at last three ways: First, we explicitly focus on models with information uncertainty; second, we use CDS spreads, which should be less sensitive to liquidity distortions; third, to our best knowledge, this is the first paper that directly extracts the equity premium out of credit prices.

Subsection A starts with the classical Merton model. We derive a simple Merton estimator for the market Sharpe ratio and the equity premium. This estimator is only based on observable parameters, i.e. the risk neutral and actual default probability, the maturity and equity correlations. Subsection B and appendix A expand this framework to first passage time models, strategic default models and models with unobservable asset values based on Duffie/Lando (2001).

## A Equity premium estimation in the Merton framework

Structural models for the valuation of debt and the determination of default probabilities are already mentioned in Black/Scholes (1973). The Merton framework presented in this subsection is based on Merton (1974), who explicitly focusses on the pricing of corporate debt. In this framework a company's debt consists of one zero-bond. Default occurs if the asset value of the company falls below the nominal value  $N$  of the zero bond at maturity of the bond. A company can therefore only default at one point in time, which obviously poses a simplification of the real world. The asset value  $V_t$  is modelled as a geometric Brownian motion with volatility  $\sigma$  and drift  $\mu = \mu_V$  (actual drift) and  $r$  (risk neutral drift) respectively, i.e.  $dV_t^P = \mu V_t dt + \sigma V_t dB_t$  and  $dV_t^Q = r V_t dt + \sigma V_t dB_t$ , where  $B_t$  denotes a standard Wiener process. In this framework, the real world default probability  $P^{def}(t, T)$  between  $t$  and  $T$  can be calculated as follows:

$$\begin{aligned} P^{def}(t, T) = P[ V_T < N ] &= P[ V_t \cdot e^{(\mu - \frac{1}{2}\sigma^2) \cdot (T-t) + \sigma \cdot (B_T - B_t)} < N ] \\ &= \Phi \left[ \frac{\ln \frac{N}{V_t} - (\mu - \frac{1}{2}\sigma^2) \cdot (T - t)}{\sigma \cdot \sqrt{T - t}} \right]. \end{aligned} \quad (1)$$

Here,  $\Phi$  denotes the cumulative standard normal distribution function. The default probability under the risk neutral measure  $Q$  can be determined accordingly as

$$Q^{def}(t, T) = Q[V_T < N] = \Phi \left[ \frac{\ln \frac{N}{V_t} - (r - \frac{1}{2}\sigma^2) \cdot (T - t)}{\sigma \cdot \sqrt{T - t}} \right]. \quad (2)$$

Combining (1) and (2) yields (cf. Duffie/Singleton (2003))

$$Q^{def}(t, T) = \Phi \left[ \Phi^{-1}(P^{def}(t, T)) + \frac{\mu - r}{\sigma} \cdot \sqrt{T - t} \right], \quad (3)$$

which can be transformed to estimate the Sharpe ratio of the companies assets ( $SR_V$ ):

$$SR_V := \frac{\mu - r}{\sigma} = \frac{\Phi^{-1}(Q^{def}(t, T)) - \Phi^{-1}(P^{def}(t, T))}{\sqrt{T - t}}, \quad (4)$$

It should be noted, that the formula is still correct if a non-stochastic, constant payout ratio  $\delta$  is introduced. Relationship (4) is a central formula in our paper. It has two main advantages that make it convenient for our purpose: First, it directly yields the Sharpe ratio of the assets, i.e. neither  $\mu_V$  and  $\sigma_V$  nor  $V_t$ ,  $N$  or  $r$  have to be estimated separately. In contrast to other applications of structural models we do not have to calibrate any parameter of the asset value process. The company Sharpe ratio can simply be estimated based on actual and risk neutral default probabilities and the maturity. Second, it is robust with respect to model changes. This will be discussed in the next subsection and in the appendix.

If we try to extract the market Sharpe ratio out of (4), we are faced with an additional problem: The Sharpe ratio of the assets  $\frac{\mu_V - r}{\sigma_V}$  will usually differ from the market Sharpe ratio, since the assets  $V_t$  will not necessarily be on the efficient frontier. The Sharpe ratio of the assets does not only capture the risk preference of investors, but also depends on the correlation of the assets with the market portfolio. The market Sharpe ratio can be calculated via a straight forward application of the continuous time CAPM:<sup>6</sup>

$$\mu_V = r + \frac{\mu_M - r}{\sigma_M} \cdot \rho_{V,M} \cdot \sigma_V \Leftrightarrow \frac{\mu_M - r}{\sigma_M} = \frac{\mu_V - r}{\sigma_V} \cdot \frac{1}{\rho_{V,M}}, \quad (5)$$

where  $\rho_{V,M}$  denotes the correlation coefficient between the asset returns and the market returns.

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<sup>6</sup>We assume  $\rho_{V,M} \neq 0$ .

Therefore we will need an estimate of the correlation between the asset value and the market portfolio. This correlation  $\rho_{V,M}$  can be approximated by the correlation between the corresponding equity return and the market return (denoted by  $\rho_{E,M}$ ), i.e. by

$$\rho_{V,M} \approx \rho_{E,M}.$$

The error of this approximation is negligible, since - within the Merton framework - the equity value of a company equals a deep-in-the-money call option on the assets. The option is deep-in-the-money, since annual default probabilities are less than 0.4% for investment grade companies and less than 10% for all obligors rated B and above. For deep-in-the-money options, gamma is approx. zero, i.e. we have an almost affine linear relationship between asset and equity value, cf. Hull (2005) for example.<sup>7</sup> Hence, the following approximation holds:

$$\frac{\mu_M - r}{\sigma_M} \approx \frac{\Phi^{-1}(Q^{def}(t, T)) - \Phi^{-1}(P^{def}(t, T))}{\sqrt{T - t}} \cdot \frac{1}{\rho_{E,M}}.$$

Therefore, we define the Merton estimator of the market Sharpe ratio as:

$$\widehat{\gamma}_{SR_M, Merton} := \frac{\Phi^{-1}(Q^{def}(t, T)) - \Phi^{-1}(P^{def}(t, T))}{\sqrt{T - t}} \frac{1}{\rho_{E,M}} \quad (6)$$

Including the (expected) volatility of the market portfolio  $\sigma_M$  yields an estimator for the equity premium:

$$\widehat{\gamma}_{EP, Merton} := \frac{\Phi^{-1}(Q^{def}(t, T)) - \Phi^{-1}(P^{def}(t, T))}{\sqrt{T - t}} \frac{\sigma_M}{\rho_{E,M}} \quad (7)$$

It is emphasized that we will need a sufficient sensitivity of the risk neutral default probability  $Q^{def}(t, T)$  with respect to the Sharpe ratio for an empirical application. Otherwise noise in the data (e.g. bid-ask-spreads, inaccuracies in determining correlations and actual default probabilities) will result in a very inaccurate estimation.

If we look, for example, at a BBB-rated obligor with a 5-year cumulative actual default probability of appr. 2.17%, the resulting model-based risk neutral default probability should be either 3.6% (for an asset Sharpe ratio of 10%) or 13% (for an asset Sharpe ratio of 40%) respectively (based on (3)). Assuming a recovery rate (RR) of 50% transforms this into a CDS spread of either 37 bp or 140 bp.<sup>8</sup> This large difference indicates that noise in the input parameters will only have a

<sup>7</sup>For reasonable parameter choices, the approximation error is less than 3% (for rating grades above B) and 1% (for investment grade ratings) respectively, details are available on request.

<sup>8</sup>Here we are using the approximation CDS-spread =  $\lambda^Q \cdot (1 - RR)$ . The risk neutral default intensity  $\lambda^Q$  is derived from the risk neutral cumulative default probability via the relationship  $Q^{def}(t, T) = 1 - e^{-\lambda^Q \cdot (T-t)}$ .

minor effect on our Sharpe ratio estimation. The sensitivity with respect to noise in different input parameters is analyzed in more detail in section VI.

## B Equity premium estimation in other frameworks

Of course, our estimator  $\widehat{\gamma}_{EP, \text{Merton}}$  for the equity premium is formally only justified in a Merton framework. Moving to more elaborated structural models of default usually has a significant impact on actual and risk neutral default probabilities. E.g. in a first-passage-time framework with zero drift in the real world, actual default probabilities are twice as high as actual default probabilities in the Merton framework for the same parametrisation ('reflection principle').

Fortunately, our estimator does not only include the actual default probability but the *difference* between (the inverse of the cumulative normal distribution function of) the risk neutral and (the inverse of the cumulative normal distribution function of) the actual default probability. This difference can be shown to be very robust with respect to model changes. Intuitively, most models introduce features (e.g. first-passage mechanism, unobservable asset values) which have an effect on both actual and risk neutral default probability in the same direction. The *difference* between actual and risk neutral default probability therefore remains almost unchanged. The only parameter that solely has an effect on the actual default probability - without influencing the risk neutral default probability - is the Sharpe ratio.

The robustness with respect to model changes is analyzed in more detail in appendix A based on a first-passage-time framework, strategic default frameworks and the Duffie/Lando (2001) framework with unobservable asset values.

## III Data sources and descriptive statistics

In each week our sample consists of the intersection of a) on-the-run companies in the CDX.NA.IG index<sup>9</sup>, b) the credit default swap (CDS) database of CMA (credit markets association) and c) the KMV EDF database. The Dow Jones CDX.NA.IG-index is the main CDS index in North America. It covers the 125 most liquid North American investment grade CDS.<sup>10</sup> We used 5-year CDS spreads to derive risk neutral default probabilities because the 5-year maturity is the most liquid one. EDFs (expected default probabilities) from Moody's KMV data base were used as a proxy for the actual default probabilities and correlations with the S&P500-index as a proxy for the correlations with the market portfolio. For all parameters, we used weekly data from the period

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<sup>9</sup>Our data sample starts in 04/2003 whereas the first CDX.NA.IG index starts in 10/2003. For the dates before 10/2003 we used the constituents of the CDX.NA.IG 1 index. The results do not materially differ if we start our sample period in 10/2003.

<sup>10</sup>Although the CDX.NA.IG index is a North American index we will frequently refer to 'U.S.' since the vast majority of constituents is based in the U.S. Only two non-U.S.-based companies are in our sample (Bombardier and Alcan (both from Canada)).



from April 2003 until June 2007.<sup>11</sup>

The 5-year CDS spreads (bid/ask/mid) used in our analysis were taken from Datastream. These data is compiled and provided by Credit Market Analysis (CMA) who collects CDS data from a range of market contributors from both buy- and sell-side institutions. Only dates with at least one trade or firm bid for the respective CDS are used to avoid potential errors from pure market maker data. We used CDS mid spreads for our analysis. The risk neutral default probability  $Q^{def}$  was derived by the approximation  $Q^{def} = \exp\left(-\frac{s}{LGD} \cdot T\right)$  out of the CDS spread  $s$  with maturity  $T$  and the risk neutral loss given default  $LGD$  (cf. Duffie/Singleton (2003) and footnote 8). A recovery rate  $(1 - LGD)$  of 45% was used and robustness tests were conducted.

We used expected default frequencies (EDFs) from Moody's KMV data base as our primary proxy for the actual default probabilities. Robustness tests based on agencies ratings and hazard rate models are provided in the robustness section. EDFs are default probabilities, which are based on a Merton-style structural framework, cf. Moody's KMV (2007). The calibration is, however, done more pragmatically based on a large set of historical data and on discriminant analysis. EDFs are widely used in the banking industry and also constitute a part of some of the internal rating systems of large banks. They have also been used in academic studies such as in Berndt et.al. (2005). We used 1-year EDFs (and the respective equivalent rating grades from Aaa to B3) and derived multi-year EDFs by Moody's cumulative default probabilities per rating grade.<sup>12</sup> The cumulative default probabilities were determined via a logarithmic approach based on raw data from Moody's (2007). The resulting table of cumulative default probabilities can be found in Appendix B. The main advantage of EDFs compared to other ratings for our purpose is its link to market data: The current asset volatility and equity value are direct input parameters, therefore EDFs constitute a 'point-in-time' estimation of the current default probability. In contrast to EDFs, the ratings of the large rating agencies are defined as 'through-the-cycle'-ratings, which - in effect - results in different default probabilities for a specific rating grade dependent on the current overall economic outlook.

We used 3-year weekly<sup>13</sup> correlations between the reference entities share price returns and the S&P-500 index. The share prices were taken from Datastream. We used median industry correlations since industry wide estimations of correlations have lower standard errors than a company by company estimation. This procedure also allowed to include companies without a

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<sup>11</sup>EDFs from KMV are only available on a monthly basis. We assumed EDFs to be constant within each month.

<sup>12</sup>Cf. Appendix B for details. Elton et.al. (2001) use a similar approach based on transition matrices. We have opted for a direct cumulative estimation because of indications that rating migrations are non-Markovian. The differences are though minimal, robustness tests based on migration matrices are available on request.

<sup>13</sup>The calibration of correlations has a minor effect on the overall result, using 2-year or 1-year correlations did not alter results significantly.

Variable	N	Mean	Median	Std. dev.	25th Perc	75th Perc
CDS mid	24,785	54.53	39.80	58.41	25.50	61.00
CDS offer	24,785	56.76	42.00	59.31	27.20	63.50
CDS bid	24,785	52.37	37.70	57.69	23.70	59.00
$\Delta(\text{bid, offer})$	24,785	4.40	4.00	3.02	3.00	5.00
EDF1	24,785	0.17%	0.07%	0.50%	0.04%	0.15%
EDF5	24,785	1.90%	1.26%	2.58%	0.85%	2.14%
$\rho$	24,785	0.52	0.53	0.08	0.46	0.59
Implied market volatility	24,785	17.14%	16.31%	2.36%	15.43%	18.80%

Table II:

**Descriptive statistics**

Descriptive statistics for input parameters. The sample consists of the intersection of the KMV database, the CDX.NA.IG on-the-run companies and the CMA CDS database (via datastream) from April 2003 to June 2007.  $EDF1/EDF5$  denote 1- and 5-year cumulative default probabilities based on KMV EDFs.  $\rho$  denotes the correlation between equity returns and S&P 500 returns. Implied market volatility is taken from the VIX term structure published by the CBOE based on mid option prices for maturities from 18-23 months.

3-year equity price history. The industry sector classification was based on the sub-indices of the CDX.NA.IG index.

Expected volatilities for the market portfolio were approximated by implied volatilities from the VIX term structure. Data was collected directly from the CBOE webpage<sup>14</sup>. We used implied volatilities based on mid options prices for maturities from 18-23 months which was the longest maturity bucket that was consistently available.

Our final data set consists of 24,785 date/company-combinations for which 5-year CDS spreads and EDFs were available. Table II gives an overview of the main input parameters.<sup>15</sup>

## IV Results

Based on the data described in section III and the Merton estimator for the equity premium (7), the company Sharpe ratio (4) and the market Sharpe ratio (6) derived in section II, we estimate the implicit equity premium and company and market Sharpe ratios for each of the 24,785 observations. Table III provides the results on a yearly basis in column (3) to (8).

<sup>14</sup>Chicago Board Option Exchange, [www.cboe.com/publish/vixtermstructure/vixtermstructure.xls](http://www.cboe.com/publish/vixtermstructure/vixtermstructure.xls).

<sup>15</sup>Based on 222 weeks in our sample period and 125 on-the-run constituents in the CDX.NA.IG index the theoretical maximum is 27,750 date/company-combinations. Therefore, we have data available for appr. 90% of the theoretical maximum. This is probably also due to the fact that we used constituents of the most liquid CDS index and our sample period starts approximately at the same time when index trading - and therefore also liquidity - took off in the CDS markets.

Table III:  
**Company Sharpe Ratio, Market Sharpe Ratio and Equity Premium Estimates based on U.S. 5-year CDS spreads from April 2003 to June 2007**

The sample consists of the intersection of the KMV database, the CDX.NA.IG on-the-run companies and the CMA CDS database (via datastream) from April 2003 to June 2007. For correlations, median industry correlations have been used based on 3-year weekly returns. Implied volatilities are based on maturities from 18-23 months from the VIX term structure (mid prices) of the CBOE.  $N$  denotes the number of weekly company/date combinations.  $s$  denotes the CDS spread,  $EDF5$  denotes the 5-year cumulative default probability based on KMV EDFs,  $\rho$  denotes the Equity/Market-correlation and  $\sigma_M$  denotes the implied S&P 500 volatility. Averages are calculated as unweighted averages over all observations.

Parameter	Year	N	Mean	Median	Std. dev.	Estimates			Mean of input parameters		
						25th Perc	75th Perc	s	EDF5	$\rho$	$\sigma_M$
Sharpe ratio company	2003	4,235	13.44%	12.47%	14.18%	5.08%	20.68%	75.10	3.72%		
	2004	5,916	16.77%	16.39%	11.52%	9.19%	23.57%	58.91	2.37%		
	2005	5,860	21.62%	20.18%	13.13%	13.33%	28.15%	57.34	1.54%		
	2006	5,835	22.52%	21.25%	12.99%	13.36%	30.29%	41.12	1.00%		
	2007	2,939	22.07%	20.21%	14.16%	12.48%	30.07%	37.10	0.82%		
	2003-2007	24,785	19.33%	18.17%	13.50%	10.63%	26.59%	54.53	1.90%		
Sharpe ratio market	2003	4,235	24.51%	21.80%	25.85%	8.36%	38.36%	75.10	3.72%	0.57	
	2004	5,916	31.77%	30.06%	22.34%	16.44%	45.81%	58.91	2.37%	0.55	
	2005	5,860	44.49%	40.83%	27.62%	25.45%	59.78%	57.34	1.54%	0.50	
	2006	5,835	46.88%	41.87%	29.49%	25.99%	63.11%	41.12	1.00%	0.50	
	2007	2,939	45.92%	40.82%	31.62%	24.72%	62.04%	37.10	0.82%	0.50	
	2003-2007	24,785	38.77%	35.30%	28.51%	19.31%	54.23%	54.53	1.90%	0.52	
Equity Premium	2003	4,235	5.16%	4.56%	5.49%	1.76%	8.02%	75.10	3.72%	0.57	20.93%
	2004	5,916	5.84%	5.53%	4.15%	2.97%	8.35%	58.91	2.37%	0.55	18.28%
	2005	5,860	7.18%	6.55%	4.54%	4.03%	9.69%	57.34	1.54%	0.50	16.04%
	2006	5,835	7.17%	6.46%	4.55%	3.91%	9.67%	41.12	1.00%	0.50	15.23%
	2007	2,939	7.08%	6.25%	4.89%	3.77%	9.59%	37.10	0.82%	0.50	15.39%
	2003-2007	24,785	6.50%	5.95%	4.74%	3.32%	9.10%	54.53	1.90%	0.52	17.14%

Our estimation yields an average equity premium of 6.50% for the U.S. market. The average company Sharpe ratio is 19.33% and the average market Sharpe ratio is 38.77%. The median values are even lower with 5.95% for the equity premium and 18.17% and 35.30% for the company and market Sharpe ratio. We would already like to mention here that all these values are upper limits for the equity premium. This is due to some implicit conservative assumptions, especially concerning the part of the CDS spread which is due to credit risk (we assume 100%) and the recovery rate (our assumption of 45% seems to be an upper limit); cf. section VI for details.

Looking at each year of our sample period separately shows a quite homogenous result: The implicit equity premium estimates range from 5.16% in 2003 to 7.18% in 2005. The year 2005 also exhibits the largest one-year increase in the equity premium up 23% from 5.84% in 2004. CDS premia were still as high in 2005 as in 2004 - especially due to an increase in spreads in the second quarter around the downgrades of Ford and General Motors - while EDFs were decreasing (2.37% vs. 1.54%) due to bullish equity markets and lower volatilities. Correlations were decreasing from 0.55 to 0.50 while implied volatilities decreased from 18.28% to 16.04% resulting in an almost unchanged term  $\frac{\sigma_M}{\rho_{E,M}}$ . It seems plausible to assume that these downgrades have led to an increase in risk aversion among market participants. We would like to point out that the implied equity premia also increased in the second quarter of 2007 at the beginning of the subprime crisis. Due to low CDS spreads in the first quarter of 2007, average estimates for the first half of 2007 are though almost the same than in 2006 (7.08% vs. 7.17%).

We would also like to emphasize the fact that our results stem from very different conditions on the credit markets. Looking at CDS spreads, they averaged 75.10 bp in the year 2003. This was accompanied by large EDFs (3.72%), large correlations (0.57) and a high implied volatility (20.93%). In the first half of 2007, spreads were less than half the spreads of 2003 (37.10 bp), EDFs were less than a fourth of their 2003 levels (0.82% vs. 3.71%), correlations were down to 0.50 and implied volatility was also significantly lower than in 2003 (15.39% vs. 20.93%). The fact that equity premium estimates were very similar throughout this time period indicates, that our estimates are not simply a result of a specific set of parameters but exhibit a certain robustness to changing market conditions. If at all, there seems to be a small tendency for equity premia to rise when credit markets are bullish (e.g. default rates and spreads decrease), although this is not or only partially true for the 2006 and 2007 period (from 2005 to 2006 Sharpe ratios increased but the implied equity premium decreased due to lower estimates for the implied volatility).

To get a first indication why these results are so robust we can decompose the spread into a part which is due to expected loss and a into a risk premium. In 2007, for example, the average cumulative actual default probability was 82 bp, i.e. the cumulative expected loss was 45 bp (using LGD=55%) and the per annum expected loss was appr. 9 bp. If we compare this expected loss

to the average spread of 37 bp we see that appr. 75% (28bp/37bp) of the spread is due to a risk premium. Doubling the risk premium while keeping the expected loss constant would require a 75% increase in the CDS spread. Doubling the risk premium by keeping the CDS spread constant is only possible with negative - and therefore unreasonable - EDFs. This intuitively indicates why our results are so robust. Small uncertainty or noise in the spread or the actual default probability simply does not significantly effect the results. We will discuss several robustness tests in more detail in section VI.

## **V Equity premium estimates for further maturities and from other markets**

We have expanded our analysis to maturities of 3, 7 and 10 years and to European and Asian reference entities, too. Maturities of 3, 5, 7 and 10 year are the standard maturities for which CDS indices are provided by 'markit'.

Using other maturities than 5 year serves several purposes: First, they offer a robustness check of our results from the previous section. On average, risk premia estimates based on 3, 7 and 10 year maturities should not largely deviate from the results of the respective 5-year maturities. Second, these results could be used to identify a term structure of risk premia. We are not aware of any empirical analysis so far which has captured risk premia term structures. Therefore, comparison to other studies is of course limited but our results could offer a starting point for the discussion.

An application of the methodology to Europe and Asia also offers several perspectives. First, the results itself are of course interesting for an estimation of equity premia on these markets. Second, the results offer a good possibility to validate the robustness of the U.S.-results. If equity markets are globally integrated, investors should demand a similar risk premium across different countries/regions. We would therefore expect equity premium estimates in a similar magnitude than based on U.S. data. Third, U.S., Europe and Asia offer a certain diversity concerning the loss experience and credit quality over our sample period. While the U.S. market was still in the aftermath of the Enron and Worldcom defaults at the beginning of our sample period and suffered the downgrades of Ford and GM in 2005, Europe did not suffer any comparable big-scale losses and had, on average, a better credit quality than the U.S. market. The Asian market did not suffer any unexpected large losses, too, but had on average a significantly lower credit quality than the U.S. market. These markets therefore offer a good opportunity to check if our estimator is robust with respect to these different credit market conditions.

Again, our data sample consists of the intersection of the KMV database, the main CDS index for the respective markets and the CMA CDS database. We used the iTraxx Europe index for

Europe and the iTraxx Asia ex Japan index for the Asian market.<sup>16</sup> Only on-the-run companies were considered. The iTraxx Europe IG index consists of 125 investment grade constituents and is rolled over every 6 months. Index trading started later than in the U.S. (June 2004 vs. October 2003). The iTraxx Asia index started with 30 constituents in July 2004, it was later enlarged to 50 constituents (effective date 9/20/2005).<sup>17</sup> Due to the later start of index trading compared with the U.S. and data availability our sample period starts at the beginning of 2004, so our sample includes the time period from January 2004 until June 2007. Again, we used the first series of the respective index to define on-the-run companies before the effective date of the first series. CDS spreads were based on the CMA database. For comparability, we included only weeks where spreads for all maturities (3, 5, 7 and 10 years) were available. Actual default probabilities were determined via EDFs from KMV. We used the same methodology as for the U.S. to transfer 1-year EDFs to cumulative default probabilities. We do though want to point out that this may be a source of inaccuracy since we assume the same migration probabilities than for the U.S. Especially for the Asian market, historical default data is rare. We are though not aware of any arguments why migration behaviour should be different for Europe or Asia compared to the U.S. However, we think that this approach gives estimates which are as close as possible to what market participants would assume. The DJStoxx 600 (Europe) and the S&P Asia 50 (Asia) were used for an estimation of correlations. Median correlations per industry sector were again used for reasons of robustness. Implicit volatilities were calculated based on the VSTOXX Volatility sub-index 24 months.<sup>18</sup> For the Asian market, implicit volatility indices are not available, therefore we used rolling 1-year historical volatilities of the S&P 50 Asia index.

Table IV provides the results for the 3-, 5-, 7- and 10-year maturities for the U.S., Europe and Asia from 2004-2007. Please note that the 5-year results for the U.S. differ slightly from the previous section since only weeks where spreads for all maturities were available have been included in this data sample.

For the U.S., results based on 3-, 7-, and 10-year maturities are similar - but slightly smaller - than for the 5-year maturities. For the 2004-2007 period the equity premium estimation based on 5-year maturities is 7.00% while the estimates for the 3-, 7- and 10-year maturities were 6.43%, 6.62% and 6.26% respectively. The market Sharpe ratio estimates range from 39.32%

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<sup>16</sup>There is also an iTraxx index covering Japan. We have chosen the iTraxx Asia ex Japan index to cover countries which seem to offer the best independent view compared with the U.S. and Europe. The biggest countries in the iTraxx Asia ex Japan are Korea, Hong Kong, Singapore, Malaysia, China and Taiwan. Together these countries offer a good perspective on a region where experience with corporate finance, derivative products and governance structures seem to be significantly different from the U.S. and Europe.

<sup>17</sup>After our sample period, effective 9/20/2007, it was again enlarged to 70 constituents.

<sup>18</sup>Implied volatilities for longer maturities are not available due to the lack of liquid option markets for longer maturities. Implied volatilities do though have the characteristic that they are less volatile for longer maturities. If at all, our results would therefore be even smoother if volatilities for longer maturities were available.

(T=10) to 43.85% (T=5). All maturities show quite similar results for each year with equity premium estimates ranging from 4.80% (T=10, 2004) to 7.33% (T=5, 2005). All maturities exhibit an increase in the implied equity premium from 2004 to 2005 while the effect for other years is quite small. These results confirm our analysis for the equity premium from the last section.

For Europe, implied equity premium estimates are lower than for the U.S. They range from 5.03% (T=3) to 5.44% (T=5). Estimates for the 7-year maturity (5.24%) and the 10-year maturity (5.06%) yield similar results. Lower equity premia for Europe compared to the U.S. are consistent with both historical experience as well as evidence from other implied equity premium estimates.<sup>19</sup> Market Sharpe ratios for Europe are also lower than for the U.S., ranging from 26.33% (T=3) to 28.39% (T=10) compared to a range of 39.32% to 43.85% for the U.S. This is also consistent with the theoretical argument that - from a global perspective - the U.S. market should be closer to the global market portfolio and therefore closer to the capital market line. The difference between estimates for the U.S. and Europe is especially pronounced in 2004 where implied equity premia estimates for Europa are as low as 1.87% (T=3). Excluding 2004 from the analysis does, however, still result in lower estimates for Europe compared to the U.S.

Average equity premia estimates for Asia are between the estimates from the U.S. and Europe. The lowest average estimates comes from the 10-year maturity (5.60%) and the highest from the 3-year maturity (6.50%) with estimates for the 5- and 7-year maturities in between (6.21% and 5.84%). The market Sharpe ratio estimates range from 35.54% to 41.40%. Again, all yearly estimates are quite similar with the lowest estimate of 4.98% (T=10, 2005) and the highest estimate of 7.63% (T=3, 2006). Interestingly, the increase in risk premia from 2004 to 2005 which occurred both for the U.S. and for Europe was much less pronounced for Asia. Market Sharpe ratios in Asia were increasing from 2004 to 2005 - but significantly less than in the U.S. and Europe - while equity premia estimates were even decreasing due to decreasing volatilities.

All in all, the results based on 3-, 7- and 10-year maturities as well as the estimates for Europe and Asia confirm the results of the previous section and even lead to smaller equity premium estimates. Again, the resulting implicit equity premia are lower than based on historical estimates.

## VI Sensitivity analysis and robustness checks

### A Sensitivity with respect to noise in input parameters

In subsection II.B and appendix A we have shown that the results are quite robust to model changes. Besides misspecifying the model, noise in the input parameters poses another possible

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<sup>19</sup>For example, Claus/Thomas (2001) estimates an equity premium of 3.40% for the U.S. while estimates for the UK, France and Germany are 2.81%, 2.60% and 2.02%.

Table IV:  
**Company Sharpe Ratio, Market Sharpe Ratio and Equity Premium Estimates based on International 3-, 5-, 7-, 10-year CDS spreads from January 2004 to June 2007**

The sample consists of the intersection of the KMV database and the major CDS indices for the U.S. (CDX.NA.IG), Europe (iTraxxEurope) and Asia (iTraxxAsia ex Japan) from January 2004 to June 2007. Only on-the-run companies are considered. CDS spreads are obtained from CMA through datastream where we included only company/date-combinations where spreads for all maturities (3-, 5-, 7- and 10-years) were available. For correlations, median industry correlations have been used based on 3-year weekly returns. Implied volatilities are based on maturities from 18-23 months from the VIX term structure (mid prices) of the CBOE for the U.S., the VSTOXX sub-index 24 months for Europe and 1-year historical volatilities for Asia.  $N$  denotes the number of CDS spreads for each maturity,  $T$  denotes the CDS maturity. Averages are calculated as unweighted averages over all observations.

Parameter	Year	U.S. N=16,761					Europe N=17,786					Asia N=3,926					
		T=3	T=5	T=7	T=10	T=3	T=5	T=7	T=10	T=3	T=5	T=7	T=10	T=3	T=5	T=7	T=10
		Sharpe ratio	2004	15.62%	16.70%	14.73%	13.79%	4.14%	6.70%	5.86%	5.54%	15.12%	15.09%	13.67%	13.13%	15.12%	15.09%
company	2005	19.86%	22.11%	20.79%	19.68%	12.36%	13.91%	13.43%	12.98%	17.59%	16.55%	15.64%	15.21%	17.59%	16.55%	15.64%	15.21%
	2006	20.75%	22.77%	21.78%	20.54%	15.61%	16.78%	16.41%	15.97%	20.65%	19.27%	17.72%	16.66%	20.65%	19.27%	17.72%	16.66%
	2007	20.67%	22.29%	22.09%	21.20%	17.00%	16.47%	16.34%	16.26%	15.38%	15.16%	15.39%	15.30%	15.38%	15.16%	15.39%	15.30%
	04-07	19.57%	21.44%	20.31%	19.22%	12.34%	13.65%	13.19%	12.83%	18.02%	17.16%	16.13%	15.50%	18.02%	17.16%	16.13%	15.50%
Sharpe ratio market	2004	29.91%	31.79%	28.08%	26.29%	8.20%	12.04%	10.57%	9.97%	31.49%	32.49%	29.69%	28.78%	31.49%	32.49%	29.69%	28.78%
	2005	40.82%	45.36%	42.63%	40.35%	26.54%	29.09%	27.96%	26.83%	40.43%	38.05%	35.94%	34.93%	40.43%	38.05%	35.94%	34.93%
	2006	43.37%	47.30%	45.19%	42.57%	33.59%	35.64%	34.80%	33.68%	49.23%	45.79%	42.04%	39.45%	49.23%	45.79%	42.04%	39.45%
	2007	43.06%	46.32%	45.91%	44.02%	36.26%	35.08%	34.65%	34.10%	34.02%	33.40%	33.71%	33.45%	34.02%	33.40%	33.71%	33.45%
	04-07	40.20%	43.85%	41.56%	39.32%	26.33%	28.39%	27.40%	26.48%	41.40%	39.43%	37.03%	35.54%	41.40%	39.43%	37.03%	35.54%
Equity Premium	2004	5.51%	5.82%	5.13%	4.80%	1.87%	2.73%	2.38%	2.24%	5.65%	5.81%	5.31%	5.15%	5.65%	5.81%	5.31%	5.15%
	2005	6.60%	7.33%	6.88%	6.51%	4.91%	5.37%	5.16%	4.94%	5.73%	5.42%	5.13%	4.98%	5.73%	5.42%	5.13%	4.98%
	2006	6.64%	7.23%	6.90%	6.50%	6.36%	6.75%	6.59%	6.37%	7.63%	7.10%	6.51%	6.10%	7.63%	7.10%	6.51%	6.10%
	2007	6.64%	7.14%	7.07%	6.78%	6.89%	6.66%	6.58%	6.48%	5.84%	5.73%	5.79%	5.74%	5.84%	5.73%	5.79%	5.74%
	04-07	6.43%	7.00%	6.62%	6.26%	5.03%	5.44%	5.24%	5.06%	6.50%	6.21%	5.84%	5.60%	6.50%	6.21%	5.84%	5.60%



source of inaccuracy. We therefore tested the sensitivity of our results with respect to all input parameters. Parameter changes of 10% relative to its original value result in an equity premium of appr. 10%/0.6 percentage points higher/lower for all parameters in our model. In addition, the sensitivity is decreasing with increasing maturity. I.e., if input parameters have the same noise for all maturities then estimates based on 10-year maturities will be more accurate than estimates based on 3-year maturities.<sup>20</sup> Of course, these sensitivities must be analyzed in combination with the accuracy of the respective input parameters. I.e. a high sensitivity is worse if the respective input parameter can not be accurately determined, it is less harmful if the respective input parameter can be determined with very little noise. We will perform various robustness tests in the following subsections.

## **B Robustness: CDS-spread**

We have used several measures to ensure that our CDS data is not significantly biased in any direction. First, our datasource (CMA) is not based on a single market participant but based on data from several buy and sell side contributors. Second, we have compared our spreads to data from Bloomberg with no significant differences. Third, we have used constituents of the most liquid indices, which should enhance liquidity and data quality for the respective constituents. In addition our data sample should be easily comparable and reproducible and is not biased towards more recent dates.

Besides specific shortcomings of OTC markets, bid/ask spreads pose a natural noise in our data. We have used mean CDS spreads in our analysis. The average bid/ask-spread is only 4 bp in our sample which is probably also due to the fact that - in each week - we have only used the 125 most liquid CDS in the market. Using bid or ask quotes changes our average equity premium by less than 5%/0.3 percentage points. Of course, some part of the CDS spread may not be attributable to credit risk. In contrast to bonds CDS are, however, seen as a rather pure measure of credit risk. E.g. Bühler/Trapp (2008) find based on a reduced-form credit risk model that the liquidity risk portions accounts for only appr. 5% of the spread. In any case, our estimate is still valid as an upper bound for the equity premium.

## **C Robustness: Recovery rate**

Based on Moody's (2007), the average recovery rate from 1982-2006 on senior unsecured bonds was 38% on an issuer-weighted basis, 37% on a value-weighted basis and 46% if each year (issuer-weighted) is given the same weight. The recovery rate volatility is significantly smaller than the default rate volatility, with a coefficient of variation of appr. 25% on a 1-year basis compared to appr. 60% for the default probability. The interquartile range for a yearly issuer-weighted recovery

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<sup>20</sup>Detailed results are available on request.

rate is 39%-54% on a 1-year basis and 43%-51% on a 5-year average basis. Altman/Kishore (1996) also estimate an average recovery rate of 48% for senior unsecured bonds. Duffee (1999) and Driessen (2003) use a recovery rate of 44%. Discussions with market participants indicated that a value of 40% for the risk neutral recovery rate is frequently used in practical applications.

Research on the recovery rates has soared over the last years, indicating that recovery rates vary by industry sector and through the business cycle. E.g., Moody's (2007) indicates a significant negative correlation between the realized recovery rate and the realized default rate. In out-of-sample tests Chava et.al. (2006) also find indications that this relationship holds true for expected recovery rates as well. These findings may affect our results in three ways: First, some of the Sharpe ratio variation over time may also be due to time-varying recovery rates. Second, the overall level of the market Sharpe ratio may be biased if the average expected recovery rate for our time period was significantly different from historical averages. Chava et.al. (2006) set up a model where the expected recovery rate can be explained by the coupon rate, the 3-month Treasury yield, the issue size and the seniority. Other covariates analyzed by Chava et.al. do not improve out-of-sample performance. Using their regression results for the expected actual recovery rate indicates again, that our recovery rate of 45% is an upper limit for the expected recovery rate.<sup>21</sup> In addition, our sample consists of CDS with maturities up to 10 years from 2003-2007 which effectively means that recovery rates from 2003-2017 - e.g. a 15-year-horizon - are relevant for our averages. On the aggregate level, this should also help to mitigate some of the effects induced by time-varying recovery rates. Third, a countercyclical time-varying recovery rate results in risk neutral recovery rates which are lower than actual recovery rates. Again, our recovery rate of 45% is an upper limit for the recovery rate.

## D Robustness: Actual default probabilities

First, it is very important to note that our main target is to determine the PD estimates that are used by market participants. E.g. if there was a better estimate for the real world default probability than that used by market participants, it could be used to exploit arbitrage opportunities but it could not be used to gauge market participants risk aversion. Market participants rely almost entirely on three types of PD estimates: agencies ratings, distance-to-default-based measures such as KMV EDFs and hazard rate models. So far we have used EDFs as our primary source for the

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<sup>21</sup>Based on Chava et.al. (2006), the expected recovery rate for senior unsecured bonds can be estimated as  $0.5183 + 0.0182 \cdot \text{couponrate} - 0.0319 \cdot 3 - \text{month} - \text{Treasury} - \text{yield} - 0.0332 \cdot \log(\text{issuesize})$ , where coupon rate and Treasury yield are measured in percentage and the issue size is measured in \$'000. Even a very conservative calibration for our purpose of ( $\text{couponrate} = 6$ ,  $3 - \text{month} - \text{Treasury} = 1$ ,  $\text{issuesize} = \$10m$ ) results in an expected recovery rate of appr. 45% (i.e. 46%). Certainly, average coupon rates have been lower than 6%, the average 3-month Treasury yield has been higher than 1% and the average issue size for our sample has been higher than 10m, therefore the abovementioned calibration is conservative for our purpose.

actual default probability. Here, we will perform robustness tests based on agencies ratings and a hazard rate model.

First, we have used agencies ratings with the corresponding cumulative default probabilities as a robustness check. Unfortunately, these ratings are through-the-cycle estimates of the default probability. Using agencies ratings therefore requires the assumption that we cover a whole economic cycle.<sup>22</sup> This assumption is probably most realistic for 5-year CDS - where we have covered the longest period from 2003-2007 including the high-expected default year 2003 - and for the longest maturity in our sample (10-year). We have averaged the ratings of Moody's, S&P and Fitch in our calculation and determined multi-period default probabilities based on appendix B. Only observations where at least one of the agencies ratings was available could be included which slightly decreased our data sample. Results are reported in Table V. For the 5-year CDS sample from 2003-2007 we estimate very similar default probabilities (1.77% vs. 1.65%) and equity premia (6.70% vs. 6.66%). The estimated equity premium based on 10-year CDS spread are even lower (5.08% (Agencies) vs. 6.35% (EDF)) but this may be due to a good credit environment from 2004-2007 - an effect which is certainly even more pronounced for shorter maturities.

Hazard rate models provide another robustness check for both 1-year and multi-year default probabilities. There is a large literature on hazard rate models for the U.S. market, e.g. Shumway (2001) and Chava/Jarrow (2004). Unfortunately, most of these models only estimate one-year ahead default probabilities and can therefore only be used as a robustness check for one-year default probabilities. Löffler/Maurer (2008) estimate a discrete duration model for conditional default probabilities up to 5 years ahead. They use accounting covariates (e.g. EBIT, total assets) as well as market variables (e.g. return, volatility) similar to Shumway (2001) for default prediction. Details about their model can be found in appendix C. For the estimates based on Löffler/Maurer (2008), we excluded financial services companies - which are excluded in their methodology - and all companies where Compustat data was not available. The results are reported in Table V. The estimates for the cumulative default probability are slightly higher resulting in slightly lower equity premia estimates, but both are very similar to the EDF model. Five (three) year cumulative default probabilities are 1.89% (0.72%) for the Löffler/Maurer model compared to 1.79% (0.59%) for the EDF model. The resulting equity premia are 6.74% (5-year) and 6.11% (3-year) compared to 6.96% (5-year) and 6.61% (3-year) for the EDF model.

Of course, accuracies for estimating equity premia in our model should always be interpreted compared to alternative techniques for estimating equity premia. An inaccuracy of 10% in the average default probability results in an increase/decrease of our equity premium estimate by appr.

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<sup>22</sup>More exactly, it requires the assumption, that investors average expectations over our sample period correctly mirror an economic cycle.

		T=3 2004-2007		T=5 2003-2007		T=7 2004-2007		T=10 2004-2007	
		EDF Model	New Model	EDF Model	New Model	EDF Model	New Model	EDF Model	New Model
Agencies	N	16,032	16,032	23,100	23,100	16,032	16,032	16,032	16,032
Rating	PD	0.58%	0.78%	1.77%	1.65%	2.25%	2.89%	3.74%	4.78%
	EP	6.52%	4.29%	6.70%	6.66%	6.71%	5.26%	6.35%	5.08%
Discrete	N	10,078	10,078	14,700	14,700				
Duration Model	PD	0.59%	0.72%	1.79%	1.89%				
	EP	6.61%	6.11%	6.96%	6.74%				

Table V:

**Equity premium estimates based on different proxies for the real world default probability**

This table shows equity premium estimates where agencies ratings and default probabilities based on a discrete duration model have been used as proxies for the real world default probability. Agencies ratings are based on average ratings of Moody's, S&P and Fitch with corresponding cumulative default probabilities based on appendix B. The discrete duration model is based on Löffler/Maurer (2008). *EDF Model* denotes the model with EDFs as proxies for the real world default probability. *New Model* denotes the model with either PDs based on agencies ratings or based on Löffler/Maurer (2008). *N* denotes the number of observations, *PD* the average cumulative default probability and *EP* the equity premium estimation. Equity premia estimations for the EDF model deviate from the previous sections due to a different sample size.

10%/0.6 percentage points. This sensitivity is comparable to the sensitivity of the long-run growth rate in dividend discount models.<sup>23</sup> In contrast to long-run growth rates we do though have (partially) objective criteria for default prediction. In addition - in contrast to dividend/earnings forecasts - default predictions are not systematically biased.

## VII Conclusion

In this paper, we have introduced a new framework for estimating the equity premium. We measure the risk attitude of investors based on credit valuations and transforms it to an equity premium via structural models of default. Intuitively, the CDS spread can be decomposed into two parts: First, a part which compensates for the expected loss. Second, a part which covers the risk premium demanded by investors. We separate these two parts and convert the risk premium into an equivalent equity premium. This approach offers a new line of thought for estimating the equity premium that is not directly linked to current methods.

We have analyzed the estimation of equity premia from credit valuations based on a simple Merton model and developed a simple estimator for the equity premium. This estimator only uses

<sup>23</sup>Based on a Gordon model the equity premium estimate in a dividend discount model is  $EP = g + d - r_f$  where  $EP$  is the equity premium estimate,  $g$  the growth rate of dividends,  $d$  the dividend yield and  $r_f$  the risk-free rate. If  $d \approx r_f$  then the sensitivity with respect to  $g$  is approx. 1.

actual and risk neutral default probabilities, the maturity and equity correlations. We do neither have to calibrate a structural model nor do we have to estimate earnings or dividend growth. The theoretical results show an astonishing robustness of this simple estimator with respect to model changes. Although actual and risk neutral default probabilities are largely affected by model changes, the Merton estimator for the Sharpe ratio is only marginally affected.

Compared to traditional DCF-models used for estimating the equity premium, CDS spreads in our model correspond to the market value of equity and actual default probabilities correspond to dividend/earnings forecasts and long-run growth assumptions. While CDS spreads and the market value of equity can both be determined with little noise, the crucial inputs are earnings- and long-run growth forecasts in the dividend-/earnings-discount models and the actual default probability in our model. There are though two decisive advantages of estimating default probabilities compared to earnings forecasts and long-run growth rates: First, they only have to be estimated up to the maturity of the respective CDS. Second, there are (at least partially) objective criteria for estimating default probabilities. For that reason different sources for the estimation of real world default probabilities have led to quite robust results.

An empirical analysis of 5-year CDS spreads from 2003-2007 of the constituents of the main CDS indices in North America, Europa and Asia yielded upper limits for the equity premium of 6.50% (North America), 5.44% (Europe) and 6.21% (Asia). Different CDS maturities (3-, 7-, 10-year) yield similar, but slightly lower, estimates for the equity premium and could provide an interesting insight on the term structure of risk premia.

As a final remark it should be pointed out that this paper proposes a new framework for estimating the equity premium based on CDS spread observations. Although we have performed several robustness checks, our approach will have to be challenged in several ways by future research. First, because of data limitations for the CDS market we have been able to analyze only a rather limited period of time and a restricted number of companies. It will be interesting to see whether the approach remains robust as presumed if a whole economic cycle as well as a larger cross-section of firms can be integrated in the analysis. Second, the literature on the estimation of expected actual default probabilities is still evolving, especially concerning multi-year default prediction. Hence, it has to be seen whether our approach will remain robust with respect to future calibrations. Third, our approach still suffers from limitations that it estimates an upper limit of the equity premium. By using methods that can split-up the CDS spread in a part due to credit risk and a part due to other factors (e.g. liquidity) the equity premium estimates could be rendered more precise.

## A Robustness of Sharpe ratio estimator with respect to model changes

In this section we will show that the Merton estimator for the Sharpe ratio is robust with respect to model changes. We will analyze the following frameworks: a first-passage-time framework based on Black/Cox (1976), a framework with unobservable asset values based on Duffie/Lando (2001) and - implicitly - all strategic default frameworks that yield a constant default barrier (e.g. Leland (1994), Leland/Toft (1996)).

**First-passage-time framework:** In a first-passage-time framework default occurs as soon as the asset value falls below the (non-stochastic, constant) default threshold. As in the Merton framework asset values  $V_t$  are assumed to follow a geometric Brownian motion but default is now modelled as the stopping time  $\tau := \inf\{s > t; V_s \leq L\}$ , where  $L \in \mathbb{R}$  denotes the default threshold. The actual ( $P^{def}(t, T)$ ) and risk neutral ( $Q^{def}(t, T)$ ) default probability can be calculated as

$$P_{FP}^{def}(t, T) = \Phi\left(\frac{b - m^P(T-t)}{\sigma\sqrt{T-t}}\right) - e^{\frac{2m^P b}{\sigma^2}} \Phi\left(\frac{b + m^P(T-t)}{\sigma\sqrt{T-t}}\right) \quad (8)$$

$$Q_{FP}^{def}(t, T) = \Phi\left(\frac{b - m^Q(T-t)}{\sigma\sqrt{T-t}}\right) - e^{\frac{2m^Q b}{\sigma^2}} \Phi\left(\frac{b + m^Q(T-t)}{\sigma\sqrt{T-t}}\right) \quad (9)$$

with  $b = \ln(\frac{L}{V_t})$ ,  $m^P = \mu - \frac{1}{2}\sigma^2$ ,  $m^Q = r - \frac{1}{2}\sigma^2$  and  $\sigma = \sigma_V$ . If either the actual or the risk neutral drift is zero, then - based on the reflection principle - the respective default probability simply equals twice the default probability of the Merton framework.

**Framework with unobservable asset values (Duffie/Lando (2001)):** The first-passage-time framework has been extended in numerous ways to better reflect the default term structure observed in the markets. These extensions include jumps in the asset value process (Zhou (1997)), an unobservable default barrier (Finger et.al. (2002)) and unobservable asset values (Duffie/Lando (2001)). We choose the Duffie/Lando model for our analysis as it is the only structural model consistent with reduced form credit pricing.<sup>24</sup> In addition, the Duffie/Lando model incorporates a sophisticated structural model of default (i.e. a strategic setting of the default barrier based on the asset value process, tax shield and insolvency costs) and - given an appropriate calibration - results in realistic default intensities for short and long term maturities.

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<sup>24</sup>The Duffie/Lando model is the only structural model so far that yields a default intensity. Defaults in a Merton framework cannot be described by default intensity processes, since the probability of a default from  $t$  (today) until  $t + \delta t$  is always zero or one for a sufficient small  $\delta t$ . A default intensity does also not exist in the Zhou (1997) framework, since the default time cannot be represented by a totally inaccessible stopping time (which is a consequence of the fact, that the default barrier may be hit/crossed by the normal diffusion process with positive probability), cf. Duffie/Lando (2001) for details.

The calculation of the cumulative default probabilities in the D/L-framework requires a weighted application of (8) and (9) over all possible asset values  $V_t$ , where the weight is - roughly speaking - the probability of the asset value  $V_t^{25}$ , i.e.<sup>26</sup>

$$P_{DL}^{def}(t, T) = \int_L^\infty \underbrace{P_{FP}^{def}(t, T, x)}_{\text{PD(first passage time) if } V_t = x} \underbrace{g^P(x|Y_t, z_0, t)}_{\text{Prob., that } V_t = x} dx \quad (10)$$

$$Q_{DL}^{def}(t, T) = \int_L^\infty Q_{FP}^{def}(t, T, x) g^Q(x|Y_t, z_0, t) dx \quad (11)$$

where  $P_{FP}^{def}(t, T, x)/Q_{FP}^{def}(t, T, x)$  denotes the actual/risk neutral probability that an asset value process starting in  $t$  at  $V_t = x$  will fall below the default barrier up to time  $T$  (cf. (8) and (9)) and  $g^P/g^Q$  is the actual/risk neutral conditional density of the asset value at  $t$  given the filtration  $\mathcal{H}_t$ .<sup>27</sup>

We will now introduce an adjustment factor which captures the difference between the Merton estimator for the Sharpe ratio and the 'true' Sharpe ratio. This adjustment factor will be defined by

$$\frac{\mu_M - r}{\sigma_M} = \gamma_{Merton} \cdot AF \quad (12)$$

where

$$\gamma_{Merton} = \frac{\Phi^{-1}(Q_{DL}^{def}(t, T)) - \Phi^{-1}(P_{DL}^{def}(t, T))}{\sqrt{T}} \cdot \frac{1}{\rho_{V,M}} = \gamma(V_t/L, \mu, r, \delta, \sigma, \alpha, t, T) \quad (13)$$

is a function of all parameters in the Duffie/Lando framework and therefore

$$AF = AF(V_t/L, \mu, r, \delta, \sigma, \alpha, t, T)$$

is also a function of the same parameters. The basic idea is now to substitute  $V_t/L$  by the actual default probability  $PD^P$ . Fixing all other parameters except  $V_t/L$ , different values for  $V_t/L$  simply result in different actual default probabilities  $PD^P$ , i.e. we can write our adjustment factor as

$$AF = AF(PD^P, \mu, r, \delta, \sigma, \alpha, t, T). \quad (14)$$

As a special case,  $\alpha = 0\%$ ,  $\delta = 0\%$  yields the classic first-passage time framework. Strategic default frameworks where the default barrier is endogeneously determined but constant are also

<sup>25</sup>Of course the probability of a single value  $V_t$  will be zero for non-degenerated parameter choices, since we operate in a continuous setting. We will still use this informal notation to allow for a better understanding.

<sup>26</sup>A detailed derivation can be found in Duffie/Lando (2001).

<sup>27</sup>Please note that the conditional density itself is dependent on the respective measure (actual/risk neutral). Intuitively, the investor in the Duffie/Lando framework 'processes' two pieces of information: First, the noisy information about the asset value. Second, the fact that no default has occurred up to time  $t$ . While the first piece of information is the same in both actual and risk neutral world, the second differs.

captured since we will simply cover any reasonable parameter combinations. I.e., for any default barrier  $L$ , we will cover all combinations which result in a rating between Aa and B and where the other parameters are within a reasonable range (see discussion below).

We have numerically evaluated (14) for all reasonable combinations of input parameters.<sup>28</sup> The calculation was carried out in four steps: In the first step, a combination of a specific rating grade and all parameters from the Duffie/Lando framework excluding the asset value  $V_t$  was chosen. Please note, that this also involves the specification of the asset Sharpe ratio in order to determine the real world drift of the asset value process. Then, based on (10), the asset value  $V_t$  was numerically determined as to result in the cumulative actual default probability for the respective rating category. Given the asset value  $V_t$  and the other parameters chosen in the first step, a straight forward application of (11) based on risk neutral parameters was used to determine the risk neutral default probability. In the fourth step, the Merton estimator (13) was calculated based on these model-based actual and risk neutral default probabilities. Comparison with the asset Sharpe ratio specified in step 1 yields the adjustment factor (based on (12)). These four steps were repeated for all reasonable parameter combinations.

The results are reported in table VI based on three scenarios: Scenario 1 restricts the asset volatility to be larger or equal to 10%. Asset volatilities below 10% are usually only observed for financial services companies. Scenario 2 captures all parameter combinations where the average default time is larger than 0.5 time the maturity. This scenario is based on a usual assumption for investment grade entities, i.e. that real world annual conditional default probabilities are an increasing function of the maturity. Scenario 3 sets the risk neutral drift of the asset value relative to the default boundary to zero. This captures the assumption of constant expected leverage. These three scenarios were designed to capture realistic parameter combinations.

Based on a 5-year maturity, the adjustment factor for investment grade entities is always between 0.85 and 1.27 in scenario 1, between 0.82 and 1.24 in scenario 2 and between 0.82 and 1.08 in scenario 3. If one does not restrict the parameter combination to one of these scenarios, very large adjustment factors may occur for some very rare parameter combination. These are combinations of a very high asset value drift combined with a low volatility. In these cases, default either happens 'very early' or never at all. Then, the difference between risk neutral and actual default probability is

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<sup>28</sup>Input parameters used were:  $\sigma$  : 3% – 30% (the 5% and 95% quantile for the asset volatility from KMV was 6% and 25% respectively), Sharpe ratio of the asset value process: 10% to 40% (The market Sharpe ratio is usually assumed to be anywhere between 20% and 50%, due to a correlation of lower than 1, the asset Sharpe ratio should be smaller),  $m$  : 0% – 5% ( $m < 0$  would imply, that the payout rate is larger than the risk free rate,  $m = 5\%$  was chosen as an upper limit to reflect (almost) zero payout at a risk free interest rate of 5%),  $\alpha$  : 0% – 30% ( $\alpha = 0\%$  reflects the classical first passage model with observable asset values, Duffie/Lando use 10% as a standard value, the upper limit of 30% is also based on Duffie/Lando(2001)),  $\hat{V}_t = V_0$  was implicitly chosen to result in the desired rating grade from Aa to B. The case  $\hat{V}_t > V_0$  and  $\hat{V}_t < V_0$  was also analyzed, the results barely differ from the case  $\hat{V}_t = Z_0$  and are available upon request. The correlation coefficient  $\rho_{V,M}$  is already captured by the asset Sharpe ratio (which is the product of market Sharpe ratio and  $\rho_{V,M}$ ).



relatively small because the investor is only exposed to systematic risk for a very short time period, afterwards the large drift and low volatility result in very low default probabilities. Apart from these unrealistic cases, the adjustment factors are very close to one and the estimator is therefore robust with respect to model changes. The results are similar for maturities of 3, 7 and 10 years.

## B Mapping of Moody's rating grades to default probabilities

For the mapping of Moody's rating grades to default probabilities and one-year EDFs to multi-year EDFs, we used the raw data provided by Moody's (2007). We used a log-linear relationship to calibrate the default probabilities, i.e. we performed the regression

$$\ln(PD) = \beta_1 + \beta_2 \cdot NRG,$$

where NRG denotes the numerical rating grade ranging from 1 (Aaa) to 16 (B3) and  $PD$  denotes the historical default probabilities per rating grade.<sup>29</sup> The resulting cumulative default probabilities are shown in table VII.

Rating	Maturity									
	1	2	3	4	5	6	7	8	9	10
Aaa	0.001	0.006	0.019	0.041	0.071	0.094	0.114	0.125	0.135	0.148
Aa1	0.002	0.011	0.032	0.065	0.108	0.143	0.173	0.190	0.205	0.224
Aa2	0.004	0.018	0.052	0.103	0.166	0.218	0.261	0.287	0.310	0.339
Aa3	0.007	0.032	0.085	0.163	0.255	0.331	0.394	0.434	0.470	0.512
A1	0.013	0.055	0.139	0.256	0.392	0.502	0.596	0.657	0.712	0.775
A2	0.024	0.095	0.228	0.404	0.601	0.763	0.900	0.995	1.078	1.173
A3	0.045	0.164	0.373	0.637	0.922	1.159	1.360	1.506	1.633	1.774
Baa1	0.083	0.285	0.611	1.004	1.416	1.760	2.056	2.278	2.475	2.683
Baa2	0.152	0.493	1.002	1.583	2.173	2.674	3.107	3.447	3.750	4.058
Baa3	0.279	0.855	1.642	2.496	3.335	4.063	4.695	5.217	5.681	6.139
Ba1	0.514	1.482	2.691	3.934	5.120	6.172	7.095	7.894	8.607	9.286
Ba2	0.946	2.569	4.411	6.202	7.858	9.376	10.722	11.946	13.041	14.046
Ba3	1.741	4.452	7.229	9.778	12.061	14.243	16.204	18.076	19.759	21.247
B1	3.204	7.716	11.847	15.414	18.512	21.638	24.488	27.354	29.936	32.139
B2	5.896	13.373	19.417	24.301	28.413	32.871	37.007	41.392	45.356	48.615
B3	10.850	23.178	31.823	38.310	43.611	49.936	55.926	62.635	68.719	73.538

Table VII:

### Cumulative default probabilities for Moody's ratings in percent

Cumulative default probabilities based on Moody's (2007) and based on a log-approach  $\ln(PD) = \beta_1 + \beta_2 \cdot NRG$ , where NRG denotes the numerical rating grade ranging from 1 (Aaa) to 16 (B3).

<sup>29</sup>The log-approach is a common approach for the calibration of default probabilities (cf. for example Bluhm et.al (2003)).

Table VI:

Maturity	Rating	$\sigma \geq 10\%$		Default Timing $\geq 50\% \cdot T$		Risk-neutral drift = 0%	
		$Min_{AF}$	$Max_{AF}$	$Min_{AF}$	$Max_{AF}$	$Min_{AF}$	$Max_{AF}$
3	Aa	0.77	1.07	0.73	1.20	0.73	1.03
	A	0.78	1.10	0.73	1.23	0.73	1.04
	Baa	0.79	1.14	0.74	1.21	0.74	1.06
	IG (Total)	0.77	1.14	0.73	1.23	0.73	1.06
5	Aa	0.85	1.14	0.82	1.24	0.82	1.05
	A	0.86	1.19	0.82	1.23	0.82	1.06
	Baa	0.87	1.27	0.84	1.21	0.84	1.08
	IG (Total)	0.85	1.27	0.82	1.24	0.82	1.08
7	Aa	0.90	1.22	0.87	1.23	0.87	1.06
	A	0.90	1.29	0.87	1.20	0.87	1.07
	Baa	0.91	1.41	0.89	1.18	0.89	1.11
	IG (Total)	0.90	1.41	0.87	1.23	0.87	1.11
10	Aa	0.93	1.34	0.91	1.23	0.91	1.07
	A	0.94	1.45	0.92	1.22	0.92	1.10
	Baa	0.95	1.62	0.94	1.17	0.94	1.14
	IG (Total)	0.93	1.62	0.91	1.23	0.91	1.14
All	IG (Total)	0.77	1.62	0.73	1.24	0.73	1.14

#### Adjustment factors in the Duffie/Lando framework

Minimum and maximum adjustment factors for investment grade ratings and maturities from 3 to 10 years.  $AF_{Min}$  and  $AF_{Max}$  denote minimum and maximum adjustment factors for the respective scenario. The scenario ' $\sigma \geq 10\%$ ' represents non-financials since asset values below 10% are usually only observed for financial services companies. The scenario 'Default Timing  $\geq 50\% \cdot T$ ' captures all parameter combinations where the average default time conditional on default up to time  $T$  ( $\tilde{\tau} := E[\tau | \tau \leq T]$ ) was larger than  $0.5 \cdot T$ . This reflects the usual assumption that for investment grade entities the real world default probability is an increasing function of the maturity. The scenario 'Risk-neutral drift = 0%' captures a frequent assumption of zero asset value drift in the risk neutral world, i.e. the expected leverage  $V_t/L$  is assumed to be constant. Rating categories and the respective mid-point PDs are from Moody's. *IG* includes all investment grade entities.

\*

## C Discrete duration model based on Löffler/Maurer (2008)

The model of Löffler/Maurer (2008) estimates cumulative default probabilities via a discrete duration model. The hazard function  $h(t)$  is defined via

$$h(t+k) = P(Y_{t+k,t+k+1} = 1 | Y_{t+k-1,t+k} = 0, X_t) = \frac{1}{1 + \exp(-\alpha_k - \beta_k X_t)}$$

where  $Y_{t+k,t+k+1} \in \{0, 1\}$  is the default indicator for the period  $(t+k, t+k+1]$  and  $X_t$  denotes the vector of covariates.  $(\alpha_k, \beta_k)$  is the vector of coefficient estimates, see table VIII below. Multi-period default probabilities can be derived via

$$P(Y_{t,t+k} = 1) = 1 - \prod_{j=0}^{k-1} (1 - h(t+j)).$$

	Prediction Horizon in Years				
	1	2	3	4	5
L	4.89*** (0.53)	2.97*** (0.41)	2.41*** (0.39)	1.49** (0.46)	0.99* (0.48)
EBIT/TA	-1.85 (1.06)	0.95 (1.16)	-0.24 (1.29)	1.86 (1.48)	2.23 (1.68)
EBIT/XINT	-0.3** (0.1)	-0.33*** (0.08)	-0.19** (0.07)	-0.29** (0.09)	-0.31*** (0.09)
SIZE	-0.18*** (0.05)	-0.2*** (0.05)	-0.19*** (0.05)	-0.22*** (0.05)	-0.21*** (0.06)
dTA	1.09** (0.39)	1.13*** (0.34)	1.12** (0.4)	1.17* (0.5)	1.37** (0.45)
RET	-1.67*** (0.31)	-0.65*** (0.18)	-0.29 (0.16)	-0.24 (0.19)	-0.11 (0.2)
VOLA	4.7*** (1.01)	4.39*** (1.11)	3.42** (1.07)	0.66 (1.36)	0.33 (1.39)
Constant	-9.05*** (0.54)	-7.53*** (0.49)	-7.08*** (0.44)	-6.47*** (0.5)	-6.12*** (0.53)

Table VIII:

### Coefficients for discrete duration model based on Löffler/Maurer (2008)

This table contains the coefficient estimates from Löffler/Maurer (2008). *L*: leverage (= Total debt / (Total debt + Marketcap)), *XINT*: interest expenses, *SIZE*: log of the market cap divided by the S&P-500 market capitalization, *dTA*: one-year asset growth, *RET*: 12-month cumulative equity return, *VOLA*: 12-month monthly equity volatility.

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